

TBM 4E, 12.6.12

Druck, Auftrieb

$$\textcircled{1} \quad F = \frac{p}{A} \Rightarrow F = p \cdot A ; 55 \text{ mm}^2 = 55 \cdot 10^{-6} \text{ m}^2$$
$$F = p \cdot A = 100 \text{ Pa} \cdot 0,000055 \text{ m} = \underline{\underline{5,5 \text{ mN}}}$$

$$\textcircled{2} \quad F_{\text{Auftrieb}} = F_G \quad V = \text{gesamtes Vol.}$$
$$\rho_W \cdot V' \cdot g = \rho_{\text{Holz}} \cdot V \cdot g \quad V' = V \text{ unter Wasser}$$
$$\frac{V'}{V} = \frac{\rho_{\text{Holz}}}{\rho_{\text{Wasser}}}$$

$$\text{a) } \frac{V'}{V} = 0,79 = \frac{\rho_{\text{Holz}}}{1000 \text{ kg/m}^3}$$
$$\underline{\underline{\rho_{\text{Holz}} = 790 \text{ kg/m}^3}}$$

$$\text{b) } \frac{V'}{V} = \frac{1000 \text{ kg/m}^3}{13546 \text{ kg/m}^3} = \underline{\underline{7,38\%}}$$

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$$m = 75'000 \text{ t} = 75 \cdot 10^6 \text{ kg}$$

$$\rho_{\text{Wasser}} = 1'020 \text{ kg/m}^3$$

$$\rho_{\text{Stahl}} = 7'850 \text{ kg/m}^3$$

$$l = 380 \text{ m}, b = 68 \text{ m}, h = 30 \text{ m}, h_{\text{max}} = 29.5 \text{ m}$$

a)  $F_G = F_{\text{Auftrieb}} = F_{G, \text{Wasser}}$

$$mg = \rho_{\text{Wasser}} \cdot V \cdot g$$

$$\Rightarrow V = \frac{mg}{\rho_{\text{W}} \cdot g} = \frac{m}{\rho_{\text{W}}} = \frac{75 \cdot 10^6 \text{ kg}}{1020 \text{ kg/m}^3}$$

$$= \underline{\underline{73'529.412 \text{ m}^3}}$$

b)  $F_{\text{res}} = F_G - F_{\text{Auftrieb}} = \frac{m}{\rho_{\text{Stahl}}} = 9'554.14 \text{ m}^3$

$$= mg - \rho_{\text{Wasser}} \cdot \frac{m}{\rho_{\text{Stahl}}} \cdot g$$

$$= g \left( m - \frac{m \cdot \rho_{\text{Wasser}}}{\rho_{\text{Stahl}}} \right)$$

$$= mg \left( 1 - \frac{\rho_{\text{Wasser}}}{\rho_{\text{Stahl}}} \right) = 640'149'363.058 \text{ N}$$

$$\approx \underline{\underline{640.15 \text{ MN}}}$$

c)  $F_G = F_A$

$$mg = \rho_{\text{W}} \cdot l \cdot b \cdot h \cdot g$$

$$h = \frac{mg}{\rho_{\text{W}} \cdot l \cdot b \cdot g} = \frac{m}{\rho_{\text{W}} \cdot l \cdot b} = \underline{\underline{2.846 \text{ m}}}$$

$$\begin{aligned}
 d) \quad g m_{\text{Ladung}} &= F_A - mg \\
 &= \rho_w \cdot l \cdot b \cdot h_{\text{max}} \cdot g - mg \\
 \Rightarrow m_{\text{Ladung}} &= \rho_w \cdot l \cdot b \cdot h_{\text{max}} - m \\
 &= 570'741'600 \text{ kg} \\
 &= \underline{\underline{570.74 \text{ kt}}}
 \end{aligned}$$

$$\begin{aligned}
 e) \quad m &= 570'741'600 \text{ kg} \\
 \rho_{\text{Öl}} &= 850 \text{ kg/m}^3 \\
 V_{\text{Öl}} &= \frac{m}{\rho_{\text{Öl}}} = 671'460.706 \text{ m}^3 \\
 &= 671'460'705.882 \text{ L} \\
 &\hat{=} 4'276'819.78 \text{ Fässer} \\
 &\hat{=} \underline{\underline{422.892 \text{ Mio. \$}}}
 \end{aligned}$$

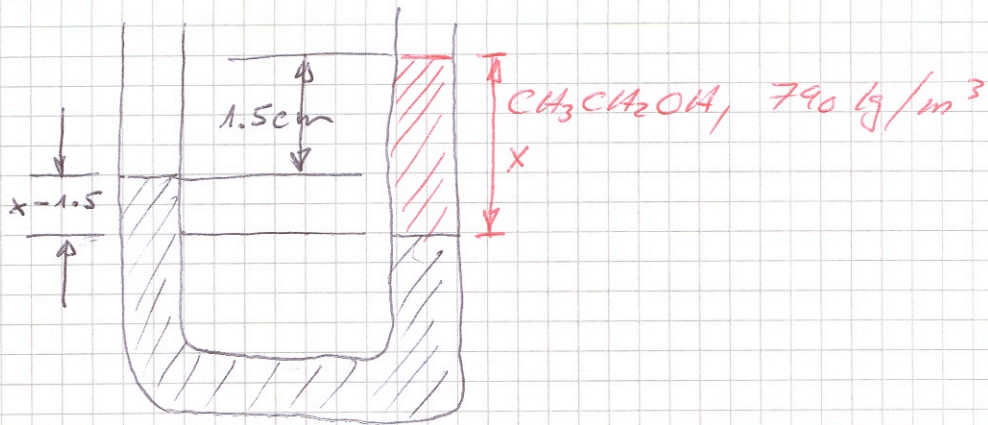
$$\textcircled{6} \quad \rho = 13'546 \text{ kg/m}^3$$

$$\begin{aligned}
 a) \quad \rho g h &= 101'325 \text{ Pa} \Rightarrow h = \frac{101'325 \text{ Pa}}{13'546 - 9.81} \\
 &= \underline{\underline{76.249 \text{ cm}}} \\
 &\hat{=} 76.25 \text{ cm}
 \end{aligned}$$

$$b) \quad \rho g h = 10 \text{ mbar} = 1000 \text{ Pa}$$

$$h = \frac{1000}{13546 - 9.81} = \underline{\underline{7.53 \text{ mm}}}$$

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$$\rho_w \cdot g (x - 0.015 \text{ m}) = \rho_A \cdot g \cdot x \quad | :g$$

$$\rho_w \cdot x - \rho_w \cdot 0.015 = \rho_A \cdot x$$

$$\rho_w \cdot x - \rho_A \cdot x = \rho_w \cdot 0.015$$

$$x = \frac{0.015 \cdot \rho_w}{\rho_w - \rho_A} = \underline{\underline{7.14 \text{ cm}}}$$

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$$V_1 = 60 \text{ L}, \quad p_1 = 2.5 \text{ atm} = 3.5 \text{ atm} \\ = 354'637.5 \text{ Pa}$$

Druck in 5m Tiefe:

$$p_2 = p_0 + \rho g h$$

$$= 101'325 \text{ Pa} + 1000 \cdot 9.81 \cdot 5$$

$$= 150'375 \text{ Pa}$$

$$p_1 V_1 = p_2 V_2$$

$$V_2 = V_1 \cdot \frac{p_1}{p_2} = \underline{\underline{141.50 \text{ L}}}$$

(- 60 Liter)